

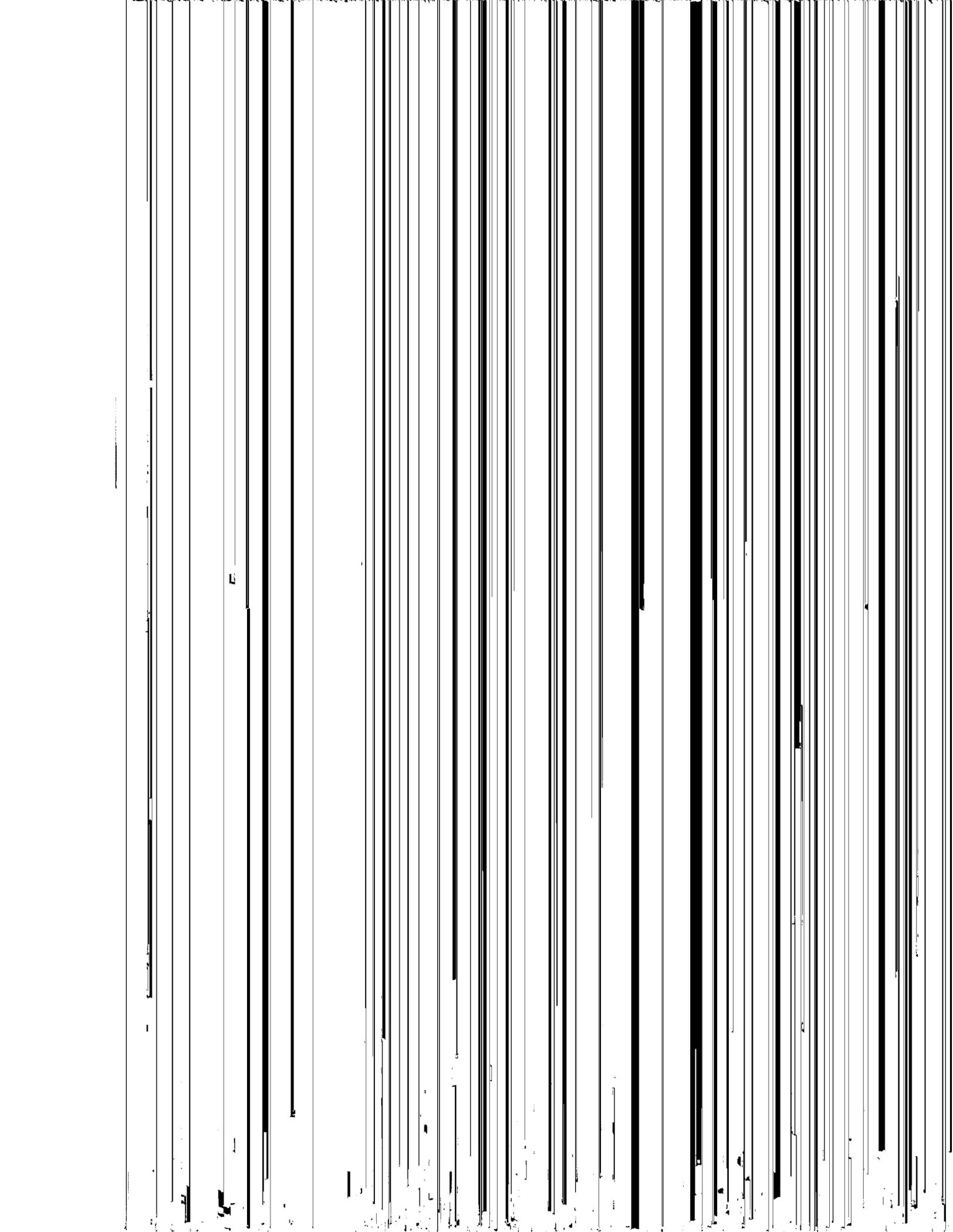
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Substitute $x =$

Substitute $x =$

The partial fra.

EXERCISES

1. $\frac{4}{(x+1)(x-5)}$

4. $\frac{5x+4}{(x+3)(x+2)}$

7. $\frac{x+2}{x^2+8x+15}$

10. $\frac{x^2-2}{(x+1)(x^2+1)}$

SOLUTIONS

1. $\frac{4}{(x+1)(x-5)}$

$x=5 \rightarrow B$

$\frac{4}{(x+1)(x-5)}$

2. $\frac{2x-3}{x^2-5x+6}$

$x=3 \rightarrow B$

$\frac{2x-3}{x^2-5x+6}$

$$3. \frac{5x}{2x^2+11x+12} = \frac{A}{2x+4}$$

$$x = -4 \rightarrow B = 4 \quad a$$

$$\frac{5x}{2x^2+11x+12} = \frac{4}{x+4}$$

$$4. \frac{5x+1}{(x+3)(x+2)(x-4)} = \frac{A}{x+2} + \frac{B}{x+3} + \frac{C}{x-4}$$

$$\rightarrow 5x+1 = A(x+2)(x-4) + B(x+3)(x-4) + C(x+3)(x+2)$$

$$x = -2 \rightarrow B = \frac{3}{2} \quad a$$

$$\frac{5x+1}{(x+3)(x+2)(x-4)} = \frac{A}{x+2} + \frac{3/2}{x+3} + \frac{C}{x-4}$$

$$5. \frac{4x^2-x+3}{(x+5)(x-1)(x-2)} = \frac{A}{x+5} + \frac{B}{x-1} + \frac{C}{x-2}$$

$$\rightarrow 4x^2-x+3 = A(x-1)(x-2) + B(x+5)(x-2) + C(x+5)(x-1)$$

$$x = 1 \rightarrow B = -1 \quad \text{and}$$

$$\frac{4x^2-x+3}{(x+5)(x-1)(x-2)} = \frac{A}{x+5} - \frac{1}{x-1} + \frac{C}{x-2}$$

$$6. \frac{2x^2-5}{x^3-2x^2-3x} = \frac{2x}{x(x+3)} + \frac{B}{x-1}$$

$$\rightarrow 2x^2-5 = A(x+3) + B(x-1)$$

$$x = -1 \rightarrow B = -\frac{3}{4}$$

$$\frac{2x^2-5}{x^3-2x^2-3x} = \frac{2}{3} \cdot \frac{1}{x} - \frac{3}{4(x-1)}$$

$$7. \frac{x+2}{x^2+8x+16} = \frac{x+2}{(x+4)^2} = \frac{A}{x+4} + \frac{B}{(x+4)^2}$$

$$x = -4 \rightarrow B = -2$$

$$\frac{x+2}{(x+4)(x+1)(x-3)} = \frac{A}{x+4} + \frac{B}{x+1} + \frac{C}{x-3}$$

8. $\frac{-}{x}$

x

x

9. $\frac{-}{(x$

\rightarrow

$x =$

$\frac{-}{(x$

10. $\frac{-}{(x$

$x =$

$\frac{-}{(x$

11. $\frac{-}{(x$

x

$\frac{-}{(x$

12. $\frac{-}{(x$

$x =$

$\frac{-}{(x$

PART B:

Integration of Pro

In this part the student
The student is also expected to use (partial fraction inspection) of the follow

In Part B each indefinite
expression into a sum of
the student. If necessary

Example 1 Find the

$$\int \frac{7x+1}{(x+3)(x-1)} dx = \int \left[\frac{5}{x+3} - \frac{4}{x-1} \right] dx$$

Example 2 Find the

$$\int \frac{6x^2+2x}{(x+3)(x-1)(x-5)} dx =$$

Example 3 Find the

$$\int \frac{1-3x}{x^3+4x^2+4x} dx = \int \frac{1-3x}{x(x+2)^2} dx$$

Example 4 Find the

$$\int \sqrt{x}$$

Exa

$$\int \sqrt{x}$$

EXE

1. \int

4. \int

7. \int

10. \int

ANS

1. \int

2. \int

3. \int

4. \int

5.

6.

7.

8.

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10.

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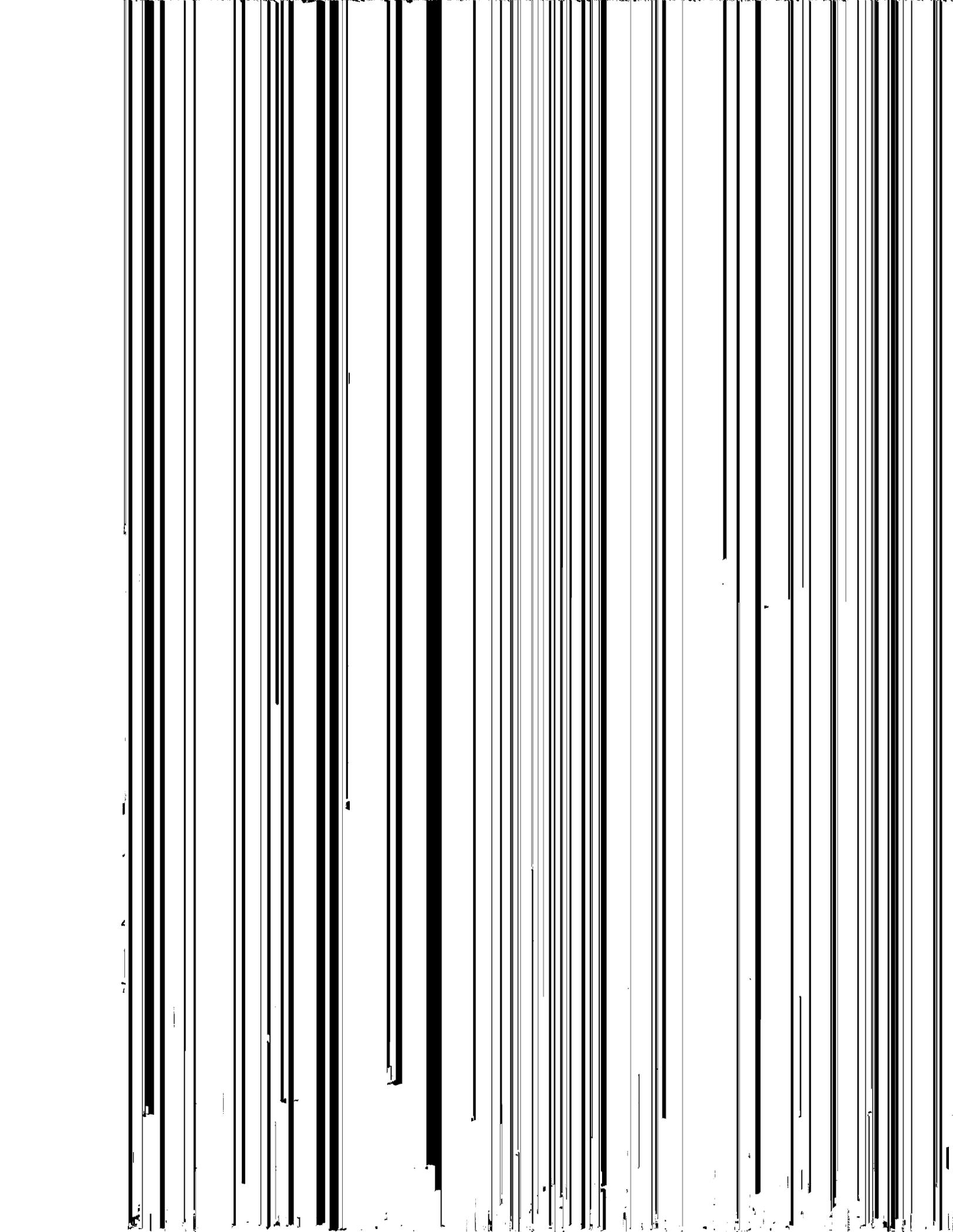
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Exa

$\int 3x$



$$9. \int \frac{x^5 - 2x^4 - 7x^3 + 20x^2}{x^3 + x^2 - 6} dx$$

$$11. \int \frac{2x^3 - 15x^2 + 17x + 2}{x^3 - 10x^2 + 25x} dx$$

ANSWERS

$$1. \int \frac{6x+5}{x+2} dx = \int \left[6 - \frac{7}{x+2} \right] dx$$

$$2. \int \frac{4x^2 - 12x - 25}{x-5} dx = \int \left[4x + 8 + \frac{15}{x-5} \right] dx$$

$$3. \int \frac{5x^3 + 3x - 2}{x-1} dx = \int \left[5x^2 + 8x + 11 + \frac{9}{x-1} \right] dx$$

$$4. \int \frac{x^3 + 3x^2 - 4x - 6}{x^2 + 2x - 15} dx = \int \left[x + 1 + \frac{9}{2} \cdot \frac{1}{x+5} + \frac{3}{2} \cdot \frac{1}{x-3} \right] dx$$

$$5. \int \frac{4x^2 - 8x + 3}{x^2 - 3x - 4} dx = \int \left[4 - \frac{3}{x+1} + \frac{3}{x-4} \right] dx = 4x - 3 \ln|x+1| + \ln|x-4| + C$$

$$6. \int \frac{x^3 - 3x^2}{x^2 - 3x - 10} dx = \int \left[x + \frac{20}{7} \cdot \frac{1}{x+2} - \frac{3}{7} \cdot \frac{1}{x-5} \right] dx = \frac{1}{2}x^2 + \frac{20}{7} \ln|x+2| - \frac{3}{7} \ln|x-5| + C$$

$$7. \int \frac{4x^3 + 20x^2 + 15x + 8}{x^3 + 5x^2 + 4x} dx = \int \left[4 + 2 \ln|x| + \ln\left| \frac{x+4}{x+1} \right| \right] dx$$

$$8. \int \frac{x^4 - 10x^3 + 28x^2 - 15x - 15}{x^3 - 7x^2 + 10x} dx = \int [x - 3$$

$$= \int \left[x - 3 - \frac{3}{2} \cdot \frac{1}{x} - \frac{1}{2} \cdot \frac{1}{x-2} - \frac{1}{x-5} \right] dx =$$

$$9. \int \frac{x^5 - 2x^4 - 7x^3 + 20x^2 - 12x + 4}{x^3 + x^2 - 6x} dx = \int [x^2$$

$$= \int \left[x^2 - 3x + 2 - \frac{2}{3} \cdot \frac{1}{x} + \frac{4}{15} \cdot \frac{1}{x+3} + \right.$$

$$\left. = \frac{1}{3}x^3 - \frac{3}{2}x^2 + 2x - \frac{2}{3}\ln|x| + \frac{4}{15}\ln|x| + \right.$$

$$10. \int \frac{4x^5 + 6x^4 + 2x^3 + 3x^2 - 5x - 7}{x^3 + 2x^2 + x} dx = \int [4x^2$$

$$= \int \left[4x^2 - 2x + 2 - \frac{7}{x} + \frac{8}{x+1} - \frac{1}{(x+1)^2} \right] dx =$$

$$= \frac{4}{3}x^3 - x^2 + 2x - 7\ln|x| + 8\ln|x+1| - \frac{1}{x+1} + C$$

$$11. \int \frac{2x^3 - 15x^2 + 17x + 25}{x^3 - 10x^2 + 25x} dx = \int \left[2 + \frac{5x^2 - 33}{x(x-5)} \right] dx =$$

$$= 2x + \ln|x| + 4\ln|x-5| + \frac{3}{x-5} + C$$

$$12. \int \frac{x^4 + 2x^3 - 6x^2 - 6x + 3}{x^3 + 4x^2 + 4x} dx = \int \left[x - 2 + \frac{-}{(x+2)^2} \right] dx =$$

$$= \int \left[x - 2 + \frac{3}{4} \cdot \frac{1}{x} - \frac{11}{4} \cdot \frac{1}{x+2} + \frac{9}{2} \cdot \frac{1}{(x+2)^2} \right] dx =$$

$$= \frac{1}{2}x^2 - 2x + \frac{3}{4}\ln|x| - \frac{11}{4}\ln|x+2| + \frac{9}{2}\ln|x+2| - \frac{9}{2(x+2)} + C$$

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