

**Dawson College**  
**Mathematics Department**

1.







2. a. [4 marks]

[4 marks] Find the average value of the function  
over the interval  $[-\pi, \pi]$ .

[3 marks] If  $f$  is continuous on  $\mathbb{R}$  show that  $\int_{-\infty}^{\infty} f(x) dx = \int_{-\infty}^{\infty} f(-x) dx$

[3 marks] Given  $\int_{-\infty}^{\infty} f(x) dx = C$ ,  $C$  - constant

Find the function  $f$

Evaluate the improper integral or show it diverges.

- a. [4 marks] \_\_\_\_\_

- b. [4 marks] \_\_\_\_\_



[4 marks] Find the area of the region enclosed by the graphs of the following functions.

Consider the region enclosed by the curve and the line

- a. [3 marks] Set up, but do not evaluate the integral for the volume of the solid when the given region is rotated about the      axis;

10. [4 marks] Determine whether the sequence converges or diverges. If it converges, find the limit.
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11. For each of the following series, determine whether the series converges or diverges. State which test you are using for each problem.

a. [4 marks]



b. [4 marks] \_\_\_\_\_

c. [4 marks] \_\_\_\_\_

12. [5 marks] Determine whether the series converges absolutely, converges conditionally, or diverges. State which test you are using.

13. [5 marks] Find the radius of convergence and the interval of convergence of the following power series.
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14. [5 marks] Find the sum of the following series if it converges or show it diverges.

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[5 marks] Find the Maclaurin series representation of

Answers:

1.
  - a. -